Benha University Faculty Of Engineering at Shoubra



ECE 122 Electrical Circuits (2)(2017/2018) Lecture (4) Paralel Resonance (P.2)

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Remember

Parallel Resonance Circuit

It is usually called tank circuit

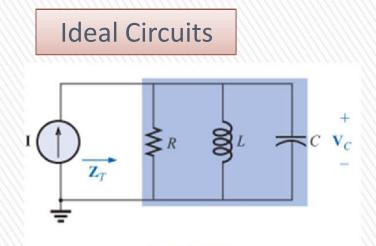


FIG. 20.21 Ideal varallel resonant network.

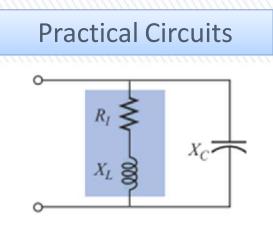
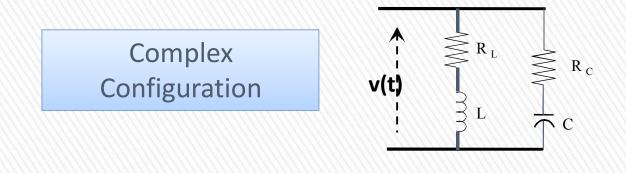


FIG. 20.22 Practical parallel L-C network.



Effect of Winding Resistance on the Parallel Resonant Frequency

- The internal resistance of the coil must be taken into consideration because it is no longer be included in a simple series or parallel combination with the source resistance and any other resistance added for design purposes.
- Even though RL is usually relatively small in magnitude compared with other resistance and reactance levels of the network, it does have an important impact on the parallel resonant condition,

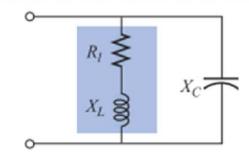


FIG. 20.22 Practical parallel L-C network.

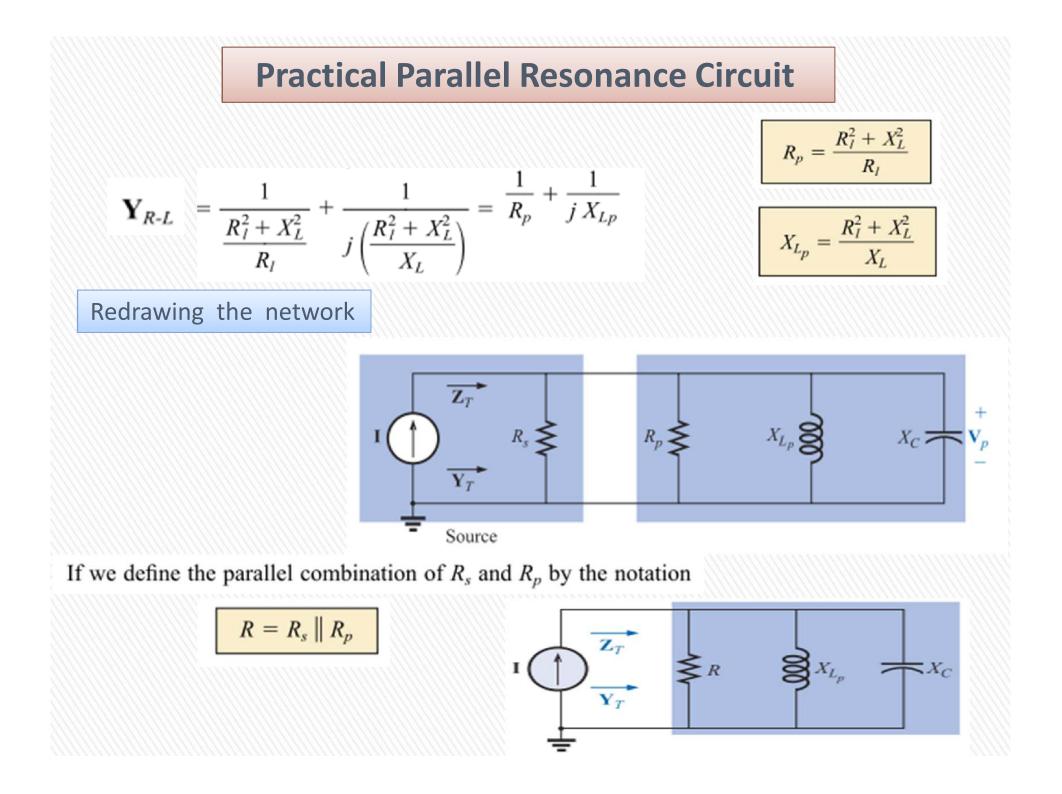
 $\mathbf{Z}_{R-L} = R_I + j X_L$

 $\mathbf{Y}_{R-L} = \frac{1}{\mathbf{Z}_{R-L}} = \frac{1}{R_l + j X_L} = \frac{R_l}{R_l^2 + X_L^2} - j \frac{X_L}{R_l^2 + X_L^2}$

1. Find a parallel network equivalent to the series R-L branch

$$R_{p} = \frac{R_{l}^{2} + X_{L}^{2}}{R_{L}} \otimes X_{L_{p}} = \frac{R_{l}^{2} + X_{L}^{2}}{R_{L}}$$

FIG. 20.23 Equivalent parallel network for a series R-L combination.



$$\mathbf{Y}_T = \frac{1}{R} + j \left(\frac{1}{X_C} - \frac{1}{X_{L_p}} \right)$$

$$\frac{1}{X_C} - \frac{1}{X_{L_p}} = 0$$
$$\frac{1}{X_C} = \frac{1}{X_{L_p}}$$

$$X_{L_p} = X_C$$

 $\frac{R_l^2 + X_L^2}{X_L} = X_C$

The resonant frequency, fp , can now be determined as follows:

$$R_l^2 + X_L^2 = X_C X_L = \left(\frac{1}{\omega C}\right) \omega L = \frac{L}{C}$$
$$X_L^2 = \frac{L}{C} - R_l^2 \qquad 2\pi f_p L = \sqrt{\frac{L}{C} - R_l^2}$$

$$f_p = \frac{1}{2\pi L} \sqrt{\frac{L}{C} - R_l^2}$$

$$f_p = \frac{1}{2\pi\sqrt{LC}}\sqrt{1 - \frac{R_I^2 C}{L}}$$

Multiplying within the square-root sign by C/L and rearranging produces :

$$f_p = f_s \sqrt{1 - \frac{R_I^2 C}{L}}$$

1. Maximum impedance

- At f = fp the input impedance of a parallel resonant circuit will be near its maximum value but not quite its maximum value due to the frequency dependence of Rp.
- The frequency at which maximum impedance will occur is:

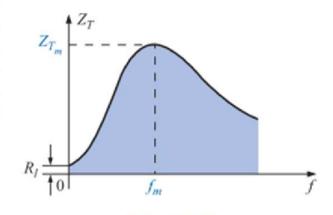
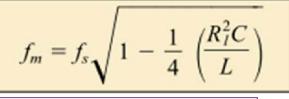


FIG. 20.26 Z_T versus frequency for the parallel resonant circuit.

fm is determined by differentiating the general

equation for ZT with respect to frequency



 $X_C >$

2. Minimum impedance

 R_{I}

XL 8

At f = 0 Hz,

Xc is O.C, XL = zero

$$Z_T = R_s \parallel R_l \cong R_l.$$

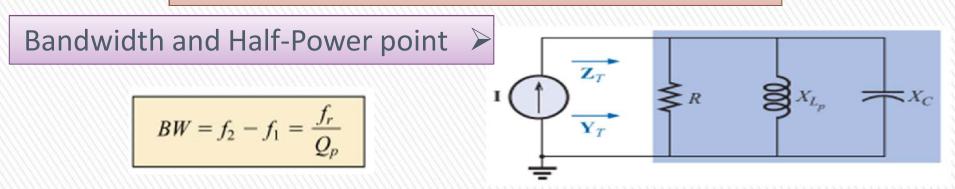
As Rs is sufficiently large for the current source (ideally infinity)

Practical parallel L-C network.

FIG. 20.22

Practical Parallel Resonance Circuit > The quality factor of the practical parallel resonant circuit determined by the ratio of the reactive \mathbf{Z}_T power to the real power at resonance 1 ($\leq R$ $Q_{p} = \frac{V_{p}^{2}/X_{L_{p}}}{V_{p}^{2}/R} \qquad R = R_{s} || R_{p},$ V_p is the voltage across the parallel branches. For the ideal current source $(R_s = \infty \Omega)$ $Q_p = \frac{R_s \parallel R_p}{X_L} = \frac{R_p}{X_L} = \frac{(R_l^2 + X_L^2)/R_l}{(R_l^2 + X_L^2)/X_L}$ $R = R_s \parallel R_p \cong R_p$ $Q_p = \frac{X_L}{R_I} = Q_I$ $R_s \gg R_p$

which is simply the quality factor Q_l of the coil.



The cutoff frequencies f1 and f2 can be determined using the equivalent network shown in the figure:

$$\mathbf{Z} = \frac{1}{\frac{1}{\frac{1}{R} + j\left(\omega C - \frac{1}{\omega L}\right)}} = 0.707R$$

$$f_1 = \frac{1}{4\pi C} \left[\frac{1}{R} - \sqrt{\frac{1}{R^2} + \frac{4C}{L}} \right]$$

$$f_{2} = \frac{1}{4\pi C} \left[\frac{1}{R} + \sqrt{\frac{1}{R^{2}} + \frac{4C}{L}} \right]$$



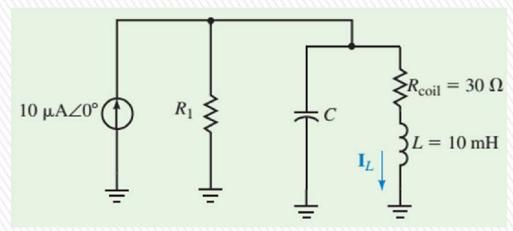
Parallel Resonance T deal circuit Practice Circuit C Rs T) RS 7 = Xit FRP 2) XL = Xc at Resonance os wp = 1 rad/s $\frac{1}{Z} = Re + J \chi_{L} \qquad J = \frac{1}{Z} = D + J D$ $Rp = Re + \chi_{L}^{2} \qquad X_{L}p = Re + \chi_{L}^{2}$ $= Re + \chi_{L}^{2} \qquad X_{L}p = Re + \chi_{L}^{2}$ $= \chi_{L} \qquad \chi_{L}$ ③ イ= = = バ+な+な $=\frac{1}{R}+j(\omega c-\overline{\omega c})$ B R=RSMRp 4) at Resonance Gi = 1 By, I in phase. Sadmittune $Yt = \frac{1}{R} + J(\frac{1}{R} - \frac{1}{dr})$ + (4) at Resonand the = the SIA $o=\left(\mathcal{F}_{p}=\left(\overline{e_{T}}\right)\right)$ 1- Re20 - 40 wp $\overline{5} \quad \overline{Q} p = \frac{R}{X_c} = \frac{R}{X_L} = \frac{\omega_P}{Bw} \left\langle \right\rangle$) fm => dZt == = R/WL = WRC S fm = 2TT/Let 1 - 2Ric $\begin{array}{c} G \\ = \omega_{g}/\Omega_{p} \end{array} = \frac{1}{RC} \quad \text{rad} \\ \end{array}$ & Max impedance at f=0 HZ NL=3) Xc oc so Zt = Rs //Re = RL

radle $G @p = \frac{R}{\chi_{Lp}} = \frac{R_s H R_p}{\chi_{Lp}}$ $Z w_1 = \frac{-1}{2RC} + \sqrt{4Rc^2} + \frac{1}{LC}$ = RSIIRP $w_2 = \frac{+1}{2RC} + \sqrt{\frac{1}{4R^2c^2}} + \frac{1}{Lc}$ -> For ideal current some (RSE) is R=RS/IRP=RP Also $Q_p = \frac{Z_{R_p}}{X_{L_p}} = \left(\frac{X_{L_s}}{R_{L_s}}\right) = Q_L$ 3) w, = wp/ 1+ (1/20)2 - w/20 Rp= RL+XL/RL W2 = wpv 1+ (22)2 + wo/29 > XLP = XL2 + Rp2/XL EBW= fr/Qp=fr-f, =wp/ap=fr-du Note For Midbaud WI=WP-BIZ W2 = + 1 2RC + V 4Ric + 1 LC WZ=Wp+B12 2 + v Cwc-I

Examples

Example (1)

Determine the values of R1and C for the resonant tank circuit of the Figure so that the given conditions are met. L=10 mH, Rcoil=30 Ω , fP=58 kHz, BW =1 kHz, Solve for the current, IL, through the inductor.



The quality factor Q_P is used to determine the total resistance of the circuit

 $R = Q_P X_C = (58)(3.644 \text{ k}\Omega) = 211 \text{ k}\Omega$

But

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_P}$$
$$\frac{1}{R_1} = \frac{1}{R} - \frac{1}{R_P} = \frac{1}{211 \text{ k}\Omega} - \frac{1}{443 \text{ k}\Omega} = 2.47 \text{ }\mu\text{S}$$

And so

 $R_1 = 405 \text{ k}\Omega$

The voltage across the circuit is determined to be

$$V = IR = (10 \ \mu A \angle 0^{\circ})(211 \ k\Omega) = 2.11 \ V \angle 0^{\circ}$$

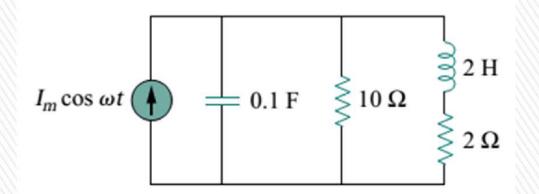
and the current through the inductor is

$$I_L = \frac{V}{R_{\text{coil}} + jX_L}$$

= $\frac{2.11 \text{ V} \angle 0^\circ}{30 + j3644 \Omega} = \frac{2.11 \text{ V} \angle 0^\circ}{3644 \Omega \angle 89.95^\circ} = 579 \ \mu\text{A} \angle -89.95^\circ$

Example (2)

Determine the resonant frequency of the circuit in Fig



Solution:

The input admittance is

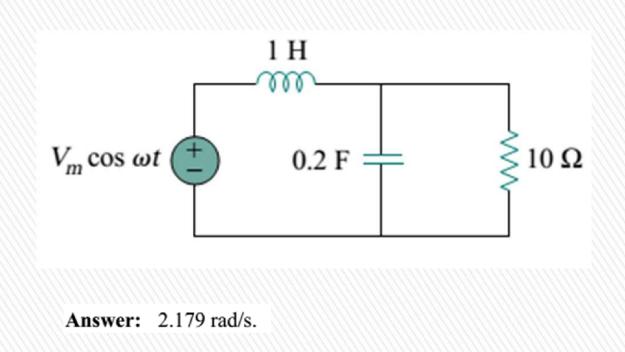
$$\mathbf{Y} = j\omega 0.1 + \frac{1}{10} + \frac{1}{2+j\omega^2} = 0.1 + j\omega 0.1 + \frac{2-j\omega^2}{4+4\omega^2}$$

At resonance, Im(Y) = 0 and

$$\omega_0 0.1 - \frac{2\omega_0}{4 + 4\omega_0^2} = 0 \qquad \Longrightarrow \qquad \omega_0 = 2 \text{ rad/s}$$

Example (3)

Calculate the resonant frequency of the circuit in Fig



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